

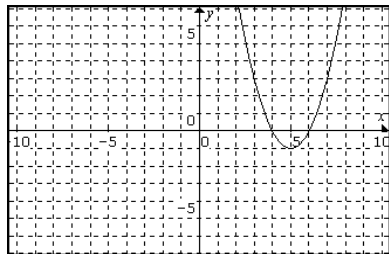
Solutions to Chapter 12

12.1

1. 5 3. 13 5. $2\sqrt{5}$ 7. 13 9. $\sqrt{13}$ 11. 6 13. $2\sqrt{2}$ 15. $\sqrt{65}$ 17. $\frac{\sqrt{13}}{12}$ 19. $\sqrt{13}$
 21. 14 23. $\sqrt{9+4a^2}$ 25. (6,6) 27. $(-\frac{1}{2}, \frac{5}{2})$ 29. $(\frac{7}{2}, 6)$ 31. $(-\frac{5}{2}, \frac{3}{2})$ 33. (3,4) 35. (6,1)
 37. (2,1) 39. (2,-3) 41. $(-\frac{27}{80}, \frac{1}{24})$ 43. $(\frac{\sqrt{6}}{2}, \frac{\sqrt{7}}{2})$ 45. $(\frac{\sqrt{8}-\sqrt{5}}{2}, \frac{\sqrt{3}-\sqrt{6}}{2})$ 47. $(\frac{p+q}{2}, \frac{p+q}{2})$

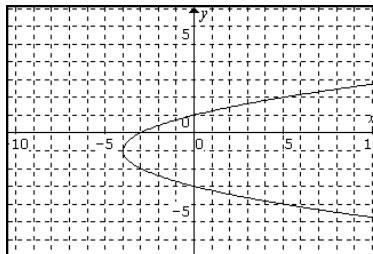
Section 12.2

1.



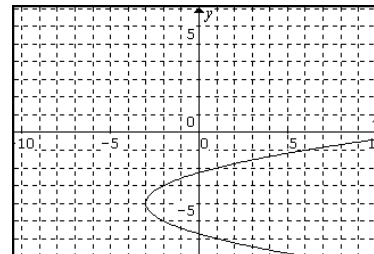
vertex: (5,-1)
 x-int: (6,0) and (4,0)
 y-int: (0,24)

3.



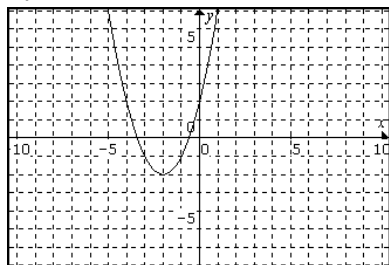
vertex: (-4,-1)
 x-int: (-3,0)
 y-int: (0,-3) and (0,1)

5.



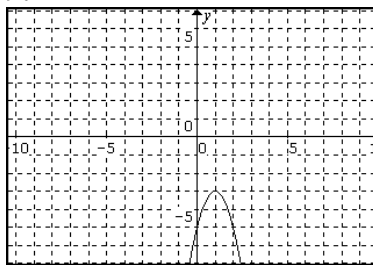
vertex: (-3,-4)
 x-int: (13,0)
 y-int:
 $(0, -4 + \sqrt{3})$ and $(0, -4 - \sqrt{3})$
 $\approx (0, -2.27) \approx (0, -5.73)$

7.



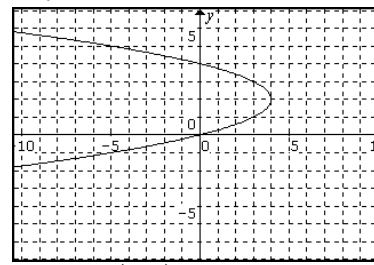
vertex: (-2,-2)
 x-int:
 $(-2 + \sqrt{2}, 0)$ and $(-2 - \sqrt{2}, 0)$
 $\approx (-0.59, 0) \approx (-3.41, 0)$
 y-int: (0,2)

9.



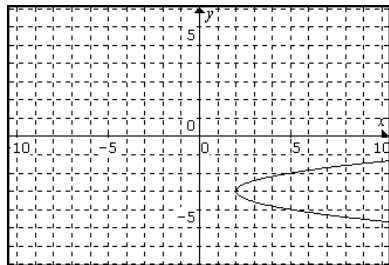
vertex: (1,-3)
 x-int: None
 y-int: (0,-5)

11.



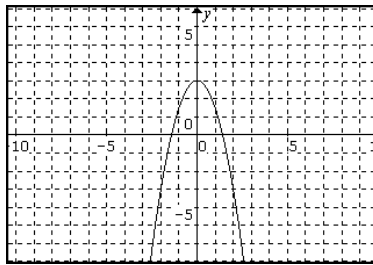
vertex: (4,2)
 x-int: (0,0)
 y-int: (0,0) and (0,4)

13.



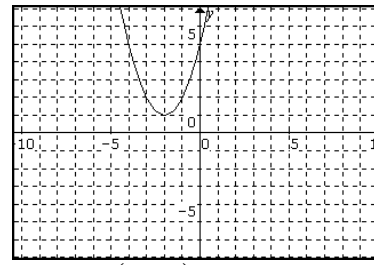
vertex: (2,-3)
 x-int: (29,0)
 y-int: None

15.



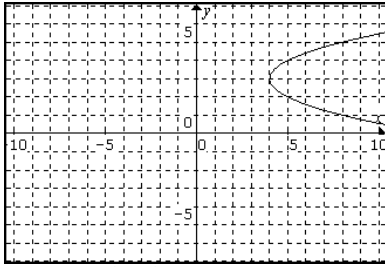
vertex: (0,3)
 x-int: $(\sqrt{2}, 0)$ and $(-\sqrt{2}, 0)$
 $\approx (1.41, 0) \approx (-1.41, 0)$
 y-int: (0,3)

17.



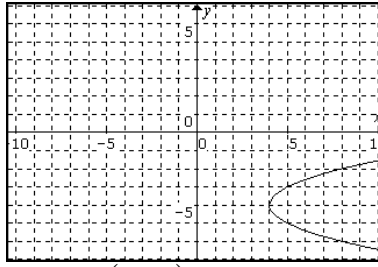
vertex: (-2,1)
 x-int: None
 y-int: (0,5)

19.



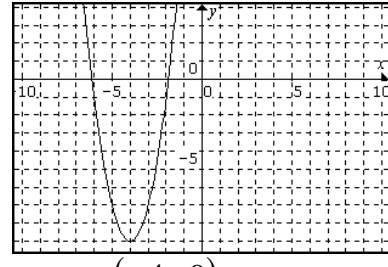
vertex: $(4, 3)$
 x-int: $(13, 0)$
 y-int: None

21.



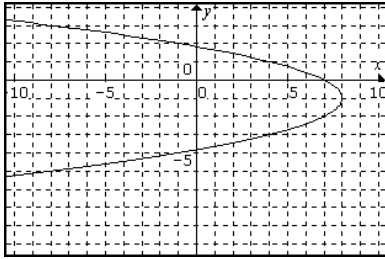
vertex: $(4, -4)$
 x-int: $(20, 0)$
 y-int: None

23.



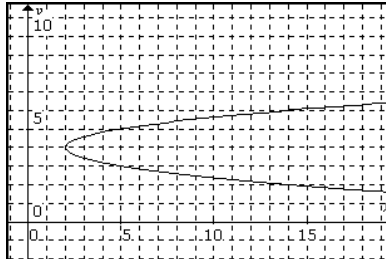
vertex: $(-4, -9)$
 x-int: $(-4 + \frac{3\sqrt{2}}{2}, 0)$ and $(-4 - \frac{3\sqrt{2}}{2}, 0)$
 $\approx (-1.88, 0) \approx (-6.12, 0)$
 y-int: $(0, 23)$

25.



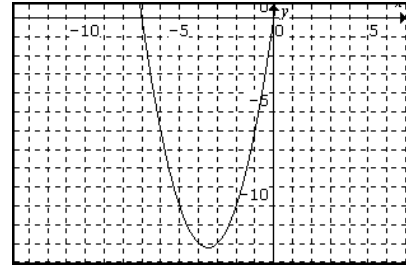
vertex: $(8, -1)$
 x-int: $(7, 0)$
 y-int:
 $(0, -1 + 2\sqrt{2})$ and $(0, -1 - 2\sqrt{2})$
 $\approx (0, 1.83) \approx (0, -3.83)$

27.



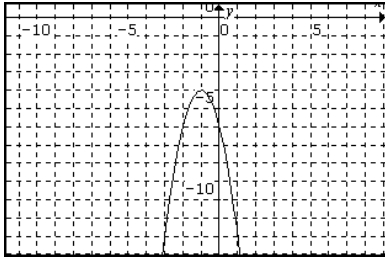
vertex: $(2, 4)$
 x-int: $(50, 0)$
 y-int: None

29.



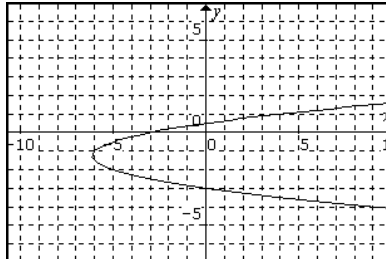
vertex: $(-\frac{7}{2}, -\frac{49}{4})$
 x-int: $(0, 0)$ and $(-7, 0)$
 y-int: $(0, 0)$

31.



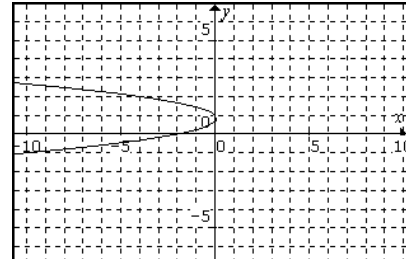
vertex: $(-1, -4)$
 x-int: None
 y-int: $(0, -6)$

33.



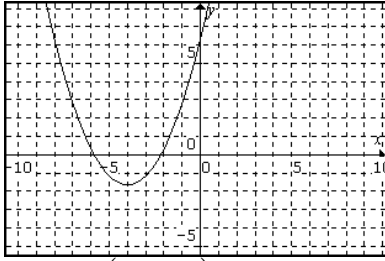
vertex: $(-\frac{49}{8}, -\frac{5}{4})$
 x-int: $(-3, 0)$
 y-int: $(0, \frac{1}{2})$ and $(0, -3)$

35.



vertex: $(\frac{1}{12}, \frac{5}{6})$
 x-int: $(-2, 0)$
 y-int: $(0, 1)$ and $(0, \frac{2}{3})$

37.



vertex: $(-4, -\frac{5}{3})$

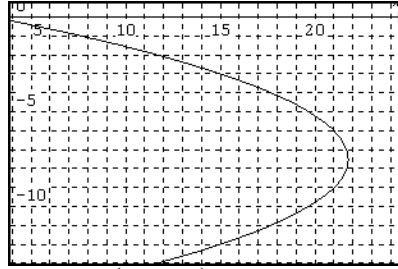
x-int:

$(\frac{-12+\sqrt{30}}{3}, 0)$ and $(\frac{-12-\sqrt{30}}{3}, 0)$

$\approx (-2.17, 0) \approx (-5.83, 0)$

y-int: $(0, \frac{19}{3})$

39.



vertex: $(\frac{87}{4}, -\frac{15}{2})$

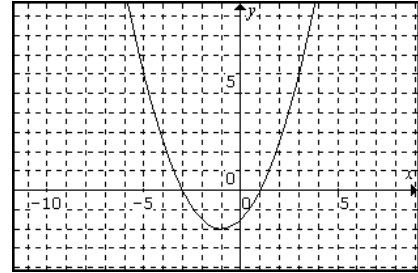
x-int: $(3, 0)$

y-int:

$(0, \frac{-15+3\sqrt{29}}{2})$ and $(0, \frac{-15-3\sqrt{29}}{2})$

$\approx (0, 0.58) \approx (0, -15.58)$

41.

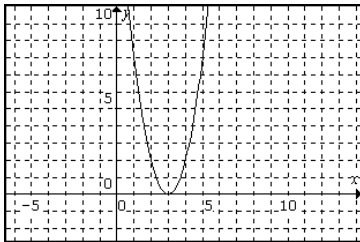


vertex: $(-1, -2)$

x-int: $(1, 0)$ and $(-3, 0)$

y-int: $(0, -\frac{3}{2})$

43.

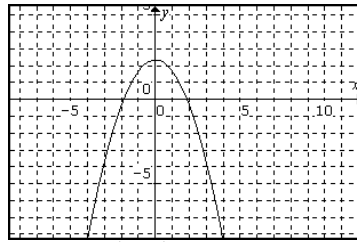


vertex: $(3, 0)$

x-int: $(3, 0)$

y-int: $(0, 18)$

45.



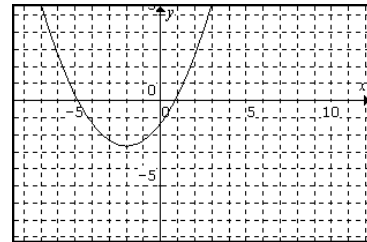
vertex: $(0, \frac{7}{3})$

x-int: $(\frac{\sqrt{14}}{2}, 0)$ and $(-\frac{\sqrt{14}}{2}, 0)$

$\approx (1.87, 0) \approx (-1.87, 0)$

y-int: $(0, \frac{7}{3})$

47.



vertex: $(-2, -\frac{8}{3})$

x-int:

$(-2+2\sqrt{2}, 0)$ and $(-2-2\sqrt{2}, 0)$

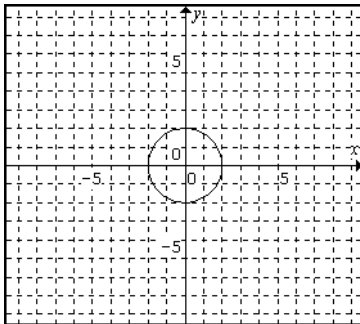
$\approx (0.83, 0) \approx (-4.83, 0)$

y-int: $(0, -\frac{4}{3})$

49. $y = 3(x+1)^2 + 3$ 51. $x = -\frac{4}{9}(y+2)^2 + 5$ 53. $x = -\frac{2}{5}(y-5)^2 + 6$ 55. $y = \frac{6}{25}(x-3)^2$

Section 12.3

1.



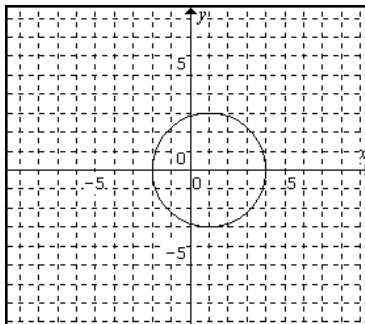
Center: $(0, 0)$

Radius: 2

x-int: $(\pm 2, 0)$

y-int: $(0, \pm 2)$

3.



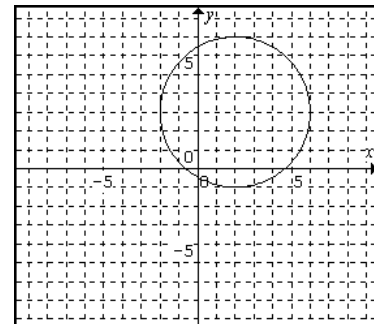
Center: $(1, 0)$

Radius: 3

x-int: $(4, 0)$ and $(-2, 0)$

y-int: $(0, \pm 2\sqrt{2}) \approx (0, \pm 2.83)$

5.



Center: $(2, 3)$

Radius: 4

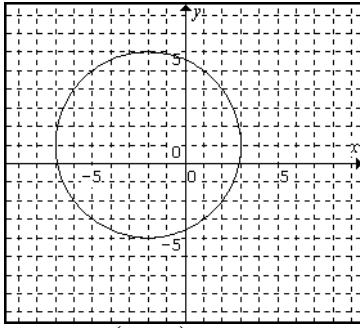
x-int: $(2+\sqrt{7}, 0) \approx (4.65, 0)$

$(2-\sqrt{7}, 0) \approx (-0.65, 0)$

y-int: $(0, 3+2\sqrt{3}) \approx (0, 6.46)$

$(0, 3-2\sqrt{3}) \approx (0, -0.46)$

7.

Center: $(-2, 1)$

Radius: 5

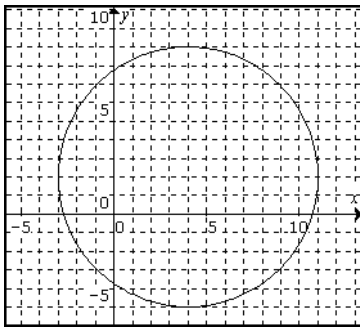
$$x\text{-int: } (-2 + 2\sqrt{6}, 0) \approx (2.9, 0)$$

$$(-2 - 2\sqrt{6}, 0) \approx (-6.9, 0)$$

$$y\text{-int: } (0, 1 + \sqrt{21}) \approx (0, 5.58)$$

$$(0, 1 - \sqrt{21}) \approx (0, -3.58)$$

13.

Center: $(4, 2)$

Radius: 7

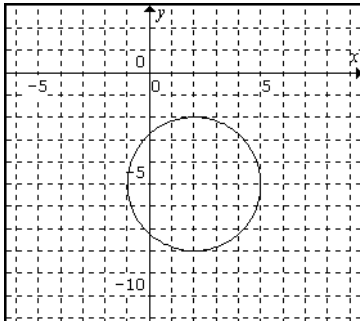
$$x\text{-int: } (4 + 3\sqrt{5}, 0) \approx (10.71, 0)$$

$$(4 - 3\sqrt{5}, 0) \approx (-2.71, 0)$$

$$y\text{-int: } (0, 2 + \sqrt{33}) \approx (0, 7.74)$$

$$(0, 2 - \sqrt{33}) \approx (0, -3.74)$$

19.

Center: $(2, -5)$

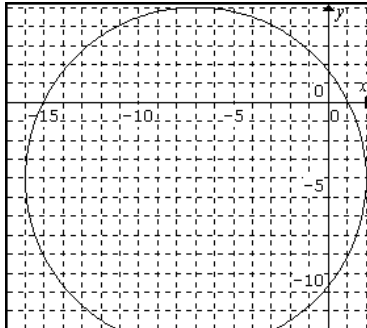
Radius: 3

No x-intercepts

$$y\text{-int: } (0, -5 + \sqrt{5}) \approx (0, -2.76)$$

$$(0, -5 - \sqrt{5}) \approx (0, -7.24)$$

9.

Center: $(-7, -4)$

Radius: 9

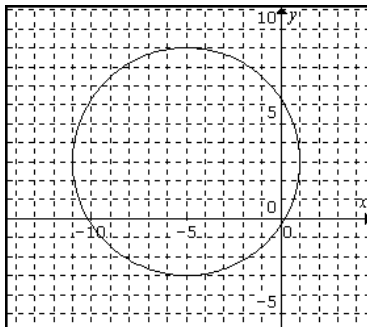
$$x\text{-int: } (-7 + \sqrt{65}, 0) \approx (1.06, 0)$$

$$(-7 - \sqrt{65}, 0) \approx (-15.06, 0)$$

$$y\text{-int: } (0, -4 + 4\sqrt{2}) \approx (0, 1.66)$$

$$(0, -4 - 4\sqrt{2}) \approx (0, -9.66)$$

15.

Center: $(-5, 3)$

Radius: 6

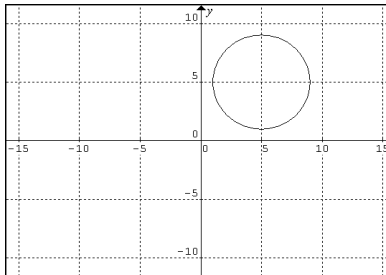
$$x\text{-int: } (-5 + 3\sqrt{3}, 0) \approx (0.20, 0)$$

$$(-5 - 3\sqrt{3}, 0) \approx (-10.20, 0)$$

$$y\text{-int: } (0, 3 + \sqrt{11}) \approx (0, 6.32)$$

$$(0, 3 - \sqrt{11}) \approx (0, -0.32)$$

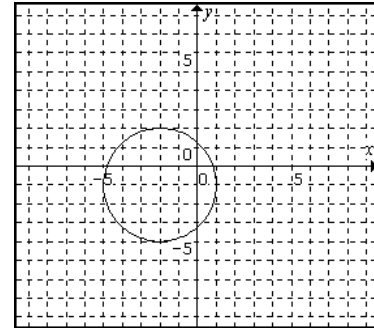
21.

Center: $(5, 5)$

Radius: 4

No x- and y-intercepts

11.

Center: $(-2, -1)$

Radius: 3

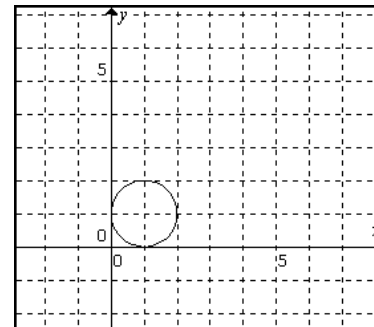
$$x\text{-int: } (-2 + 2\sqrt{2}, 0) \approx (0.83, 0)$$

$$(-2 - 2\sqrt{2}, 0) \approx (-4.83, 0)$$

$$y\text{-int: } (0, -1 + \sqrt{5}) \approx (0, 1.24)$$

$$(0, -1 - \sqrt{5}) \approx (0, -3.24)$$

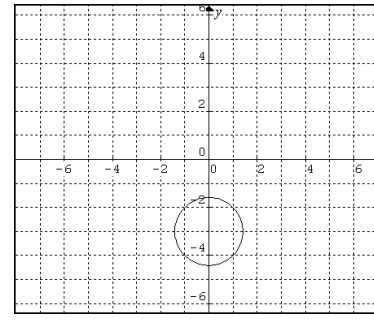
17.

Center: $(1, 1)$

Radius: 1

x-int: $(1, 0)$ y-int: $(0, 1)$

23.

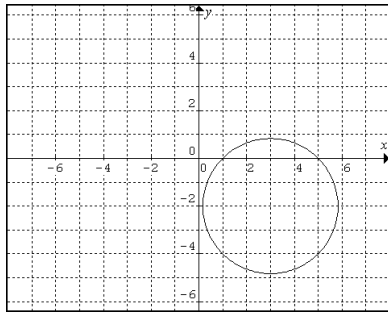
Center: $(0, -3)$ Radius: $\sqrt{2}$

No x-intercepts

$$y\text{-int: } (0, -3 + \sqrt{2}) \approx (0, -1.59)$$

$$(0, -3 - \sqrt{2}) \approx (0, -4.41)$$

25.



Center: (3, -2)

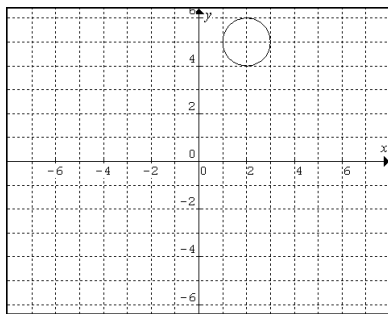
Radius: $2\sqrt{2}$

x-int: (5, 0), (1, 0)

No y-intercepts

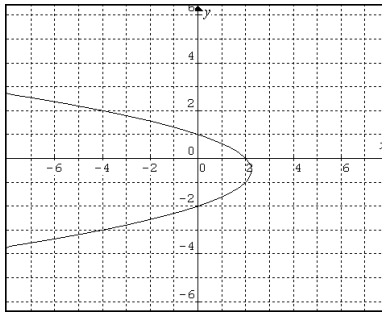
31.

Circle



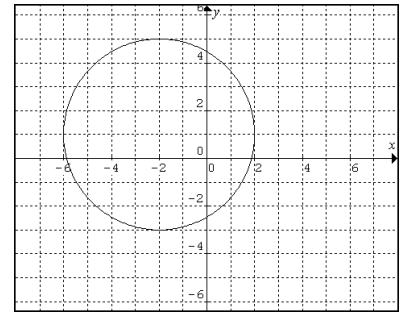
27.

Parabola



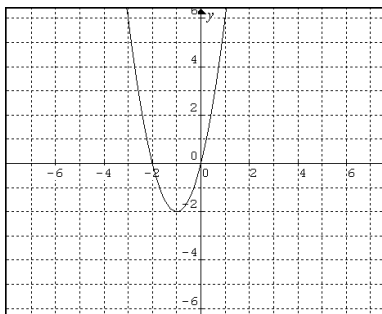
29.

Circle



33.

Parabola



35. $(x+1)^2 + (y-3)^2 = 9$

37. $(x+1)^2 + (y-1)^2 = 25$

39. $(x-1)^2 + (y-\frac{5}{2})^2 = \frac{25}{4}$

41. $(x+2)^2 + (y-1)^2 = 20$

43. $25\pi \approx 78.5$

45. $16\pi \approx 50.3$

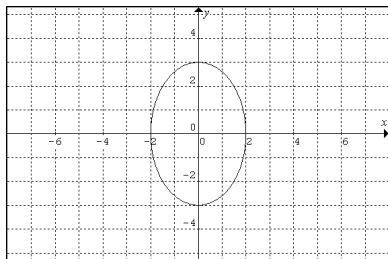
47. $36\pi \approx 113.1$

49. $\pi \approx 3.14$

51. $5\pi \approx 15.7$

Section 12.4

1.



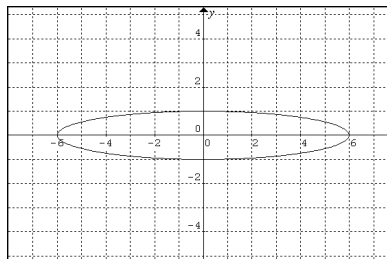
Center: (0, 0)

Vert: (0, 3), (0, -3)

x-int: (2, 0), (-2, 0)

y-int: (0, 3), (0, -3)

3.



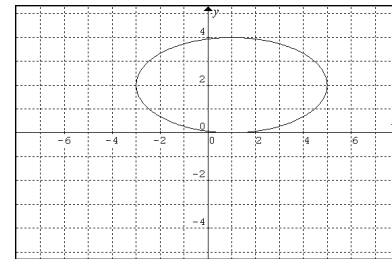
Center: (0, 0)

Vert: (6, 0), (-6, 0)

x-int: (6, 0), (-6, 0)

y-int: (0, 1), (0, -1)

5.



Center: (1, 2)

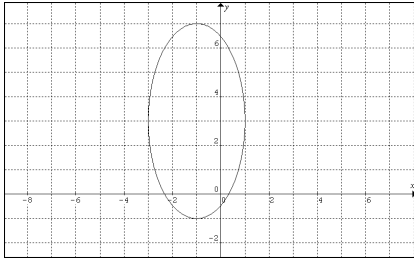
Vert: (5, 2), (-3, 2)

x-int: (1, 0)

y-int:

$(0, 2 \pm \frac{\sqrt{15}}{2}) \approx (0, 3.9), (0, 0.1)$

7.



Center: (-1, 3)

Vert: (-1, -1), (-1, 7)

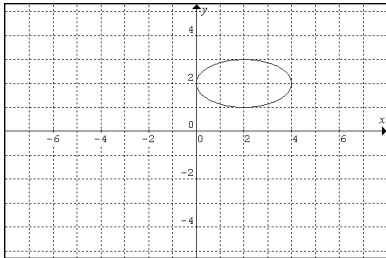
x-int:

$$\left(-1 \pm \frac{\sqrt{7}}{2}, 0\right) \approx (-2.3, 0), (0.3, 0)$$

y-int:

$$(0, 3 \pm 2\sqrt{3}) \approx (0, 6.5), (0, -0.5)$$

13.



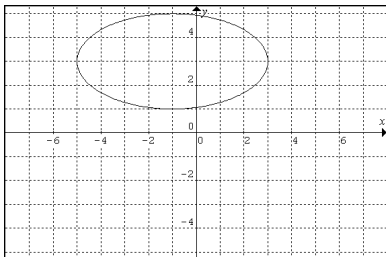
Center: (2, 2)

Vert: (0, 2), (4, 2)

x-int: none

y-int: (0, 2)

19.



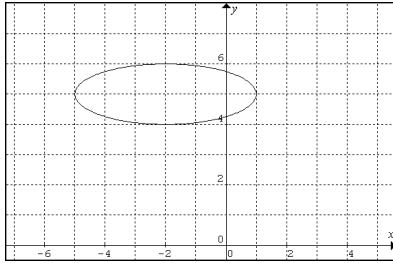
Center: (-1, 3)

Vert: (3, 3), (-5, 3)

x-int: none

$$\text{y-int: } \left(0, 3 \pm \frac{\sqrt{15}}{2}\right) \approx (0, 4.9), (0, 1.1)$$

9.



Center: (-2, 5)

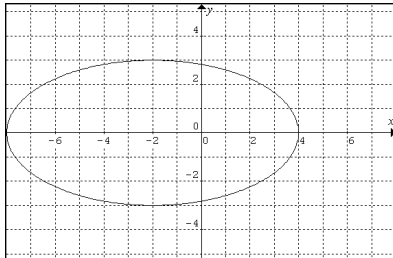
Vert: (1, 5), (-5, 5)

x-int: none

y-int:

$$\left(0, 5 \pm \frac{\sqrt{5}}{3}\right) \approx (0, 5.7), (0, 4.3)$$

15.



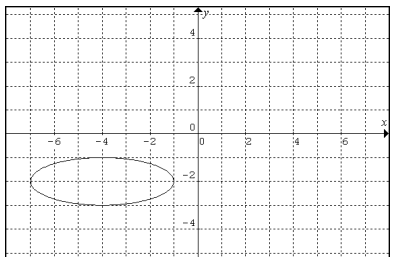
Center: (-2, 0)

Vert: (-8, 0), (4, 0)

x-int: (-8, 0), (4, 0)

$$\text{y-int: } (0, \pm 2\sqrt{2}) \approx (0, \pm 2.8)$$

21.



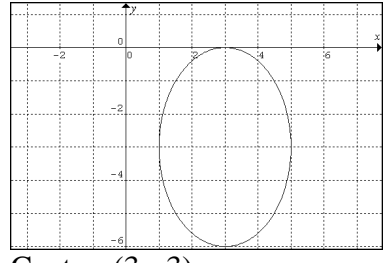
Center: (-4, -2)

Vert: (-1, -2), (-7, -2)

x-int: none

y-int: none

11.



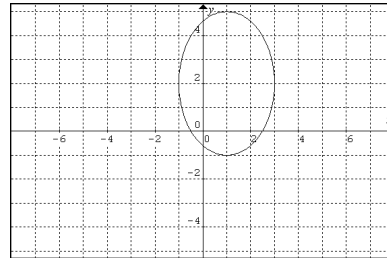
Center: (3, -3)

Vert: (3, 0), (3, -6)

x-int: (3, 0)

y-int: none

17.



Center: (1, 2)

Vert: (1, 5), (1, -1)

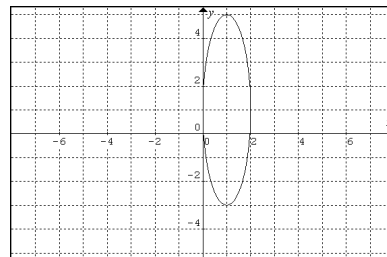
x-int:

$$\left(1 \pm \frac{2\sqrt{5}}{3}, 0\right) \approx (2.5, 0), (-0.5, 0)$$

y-int:

$$\left(0, 2 \pm \frac{3\sqrt{3}}{2}\right) \approx (0, 4.6), (0, -0.6)$$

23.



Center: (1, 1)

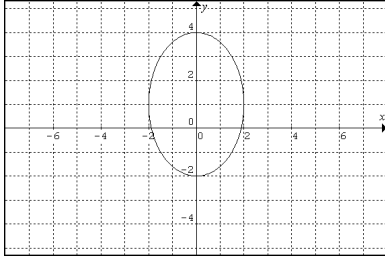
Vert: (1, 5), (1, -3)

x-int:

$$\left(1 \pm \frac{\sqrt{15}}{4}, 0\right) \approx (0.03, 0), (1.97, 0)$$

y-int: (0, 1)

25.



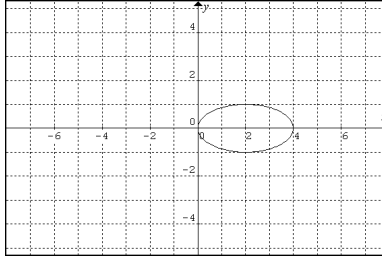
Center: (0, 1)

Vert: (0, -2), (0, 4)

x-int: $\left(\pm \frac{4\sqrt{2}}{3}, 0\right) \approx (\pm 1.9, 0)$

y-int: (0, -2), (0, 4)

27.



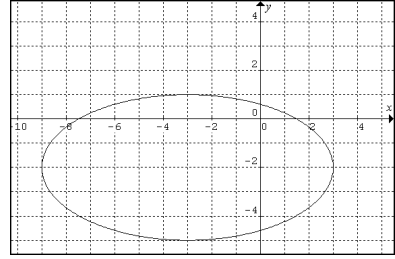
Center: (2, 0)

Vert: (0, 0), (4, 0)

x-int: (0, 0), (4, 0)

y-int: (0, 0)

29.



Center: (-3, -2)

Vert: (3, -2), (-9, -2)

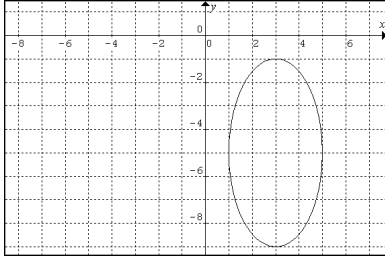
x-int:

$\left(-3 \pm 2\sqrt{5}, 0\right) \approx (-7.5, 0), (1.5, 0)$

y-int:

$\left(0, -2 \pm \frac{3\sqrt{3}}{2}\right) \approx (0, -4.6), (0, 0.6)$

31.



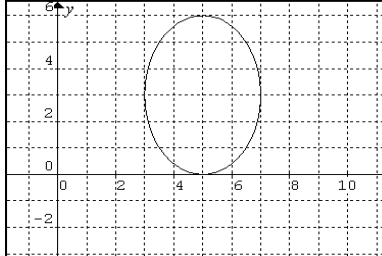
Center: (3, -5)

Vert: (3, -1), (3, -9)

x-int: none

y-int: none

33.



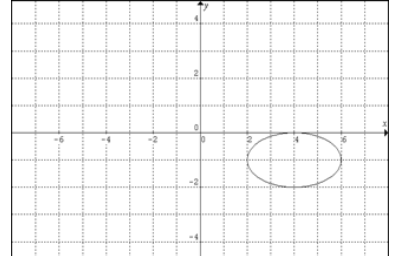
Center: (5, 3)

Vert: (5, 0), (5, 6)

x-int: (5, 0)

y-int: none

35.



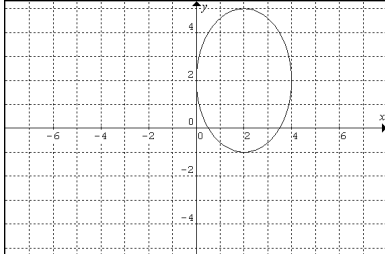
Center: (4, -1)

Vert: (6, -1), (2, -1)

x-int: (4, 0)

y-int: none

37.



Center: (2, 2)

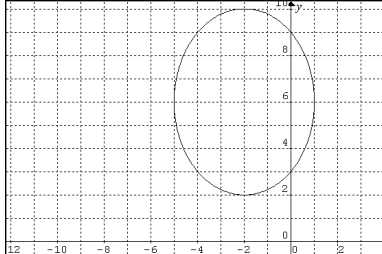
Vert: (2, 5), (2, -1)

x-int:

$\left(2 \pm \frac{2\sqrt{5}}{3}, 0\right) \approx (3.5, 0), (0.5, 0)$

y-int: (0, 2)

39.



Center: (-2, 6)

Vert: (-2, 2), (-2, 10)

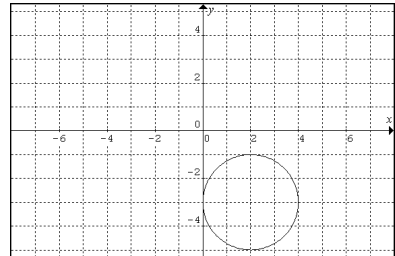
x-int: none

y-int:

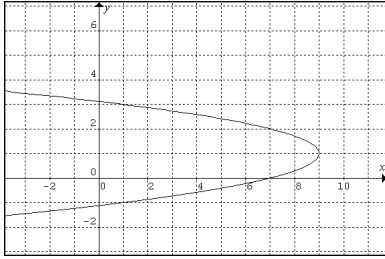
$\left(0, 6 \pm \frac{4\sqrt{5}}{3}\right) \approx (0, 8.98), (0, 3.02)$

41.

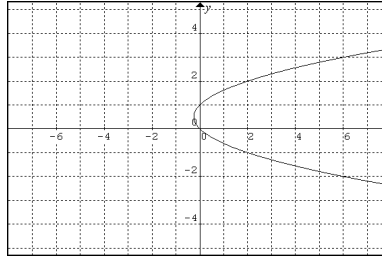
Circle



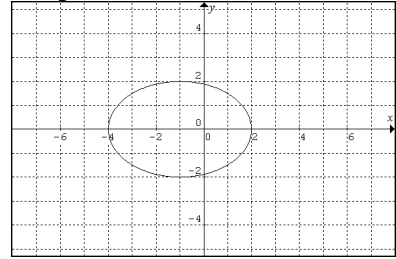
43.
Parabola



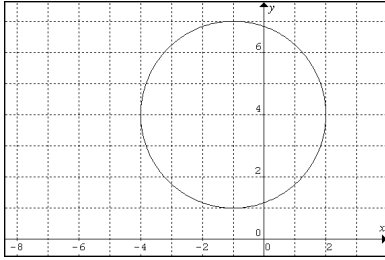
45.
Parabola



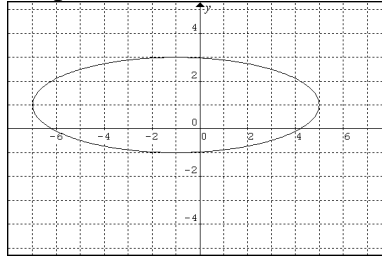
47.
Ellipse



49.
Circle



51.
Ellipse



53. $\frac{(x-2)^2}{4} + \frac{(y+3)^2}{9} = 1$ **55.** $\frac{(x-2)^2}{9} + \frac{5(y+4)^2}{9} = 1$ **57.** $\frac{(x-1)^2}{4} + (y-2)^2 = 1$

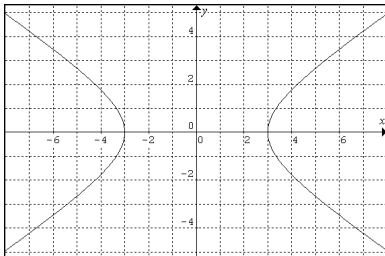
59. $8\pi \approx 25.1$

61. $6\pi \approx 18.8$

63. $2\pi \approx 6.3$

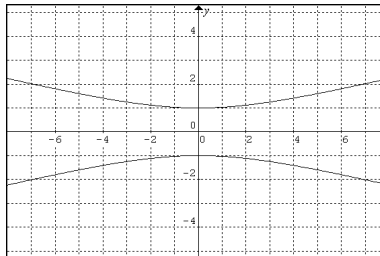
Section 12.5

1.



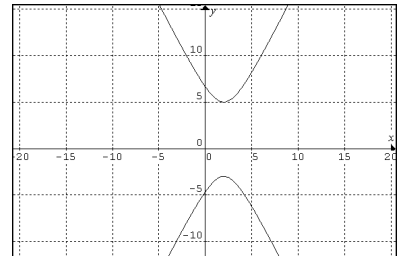
Center: (0, 0)
Vert: (3, 0), (-3, 0)
x-int: (3, 0), (-3, 0)
y-int: none

3.



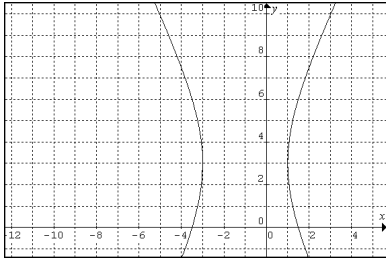
Center: (0, 0)
Vert: (0, 1), (0, -1)
x-int: none
y-int: (0, 1), (0, -1)

5.



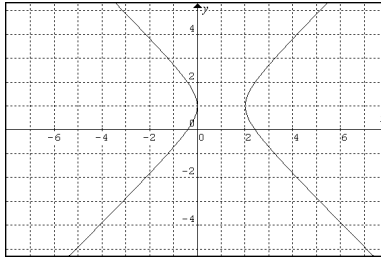
Center: (2, 1)
Vert: (2, 5), (2, -3)
x-int: none
y-int:
 $(0, 1 \pm 4\sqrt{2}) \approx (0, 6.7), (0, -4.7)$

7.



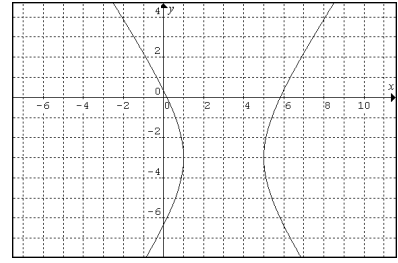
Center: $(-1, 3)$
 Vert: $(-3, 3), (1, 3)$
 x-int: $(-3.5, 0), (1.5, 0)$
 y-int: none

9.



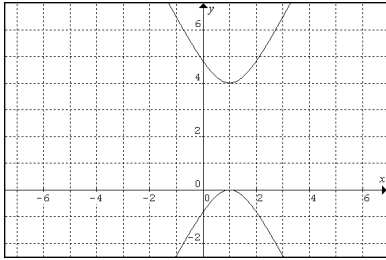
Center: $(1, 1)$
 Vert: $(0, 1), (2, 1)$
 x-int:
 $(1 \pm \sqrt{2}, 0) \approx (2.4, 0), (-0.4, 0)$
 y-int: $(0, 1)$

11.



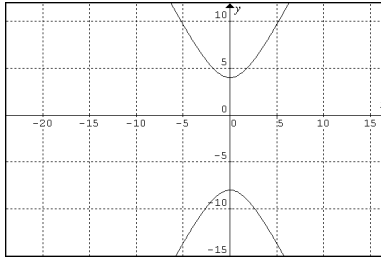
Center: $(3, -3)$
 Vert: $(5, -3), (1, -3)$
 x-int:
 $(3 \pm 2\sqrt{2}, 0) \approx (5.8, 0), (0.2, 0)$
 y-int:
 $(0, -3 \pm \frac{3\sqrt{5}}{2}) \approx (0, -6.4), (0, 0.4)$

13.



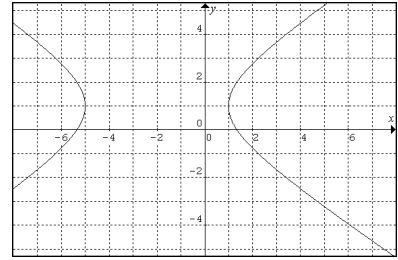
Center: $(1, 2)$
 Vert: $(1, 0), (1, 4)$
 x-int: $(1, 0)$
 y-int:
 $(0, 2 \pm 2\sqrt{2}) \approx (0, -0.8), (0, 4.8)$

15.



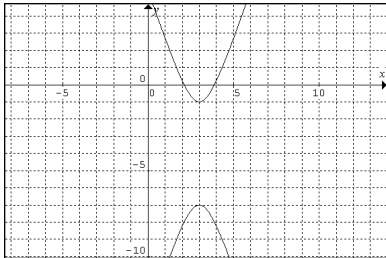
Center: $(0, -2)$
 Vert: $(0, 4), (0, -8)$
 x-int: none
 y-int: $(0, 4), (0, -8)$

17.



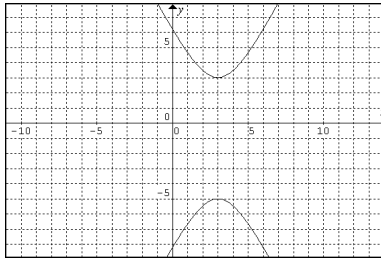
Center: $(-2, 1)$
 Vert: $(1, 1), (-5, 1)$
 x-int:
 $(-2 \pm \frac{3\sqrt{5}}{2}, 0) \approx (-5.4, 0), (1.4, 0)$
 y-int: none

19.



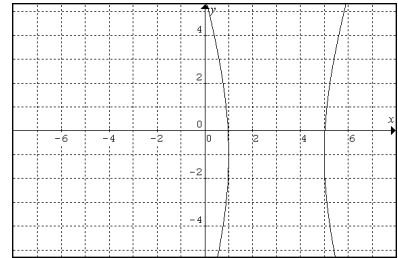
Center: $(3, -4)$
 Vert: $(3, -1), (3, -7)$
 x-int:
 $(3 \pm \frac{\sqrt{7}}{3}, 0) \approx (3.9, 0), (2.1, 0)$
 y-int:
 $(0, -4 \pm 3\sqrt{10}) \approx (0, -13.5), (0, 5.5)$

21.



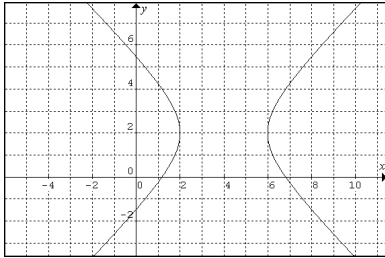
Center: $(3, -1)$
 Vert: $(3, 3), (3, -5)$
 x-int: none
 y-int:
 $(0, -1 \pm 2\sqrt{13}) \approx (0, -8.2), (0, 6.2)$

23.



Center: $(3, -1)$
 Vert: $(5, -1), (1, -1)$
 x-int:
 $(3 \pm \frac{\sqrt{37}}{3}, 0) \approx (5.03, 0), (0.97, 0)$
 y-int:
 $(0, -1 \pm 3\sqrt{5}) \approx (0, -7.7), (0, 5.7)$

25.



Center: (4, 2)

Vert: (6, 2), (2, 2)

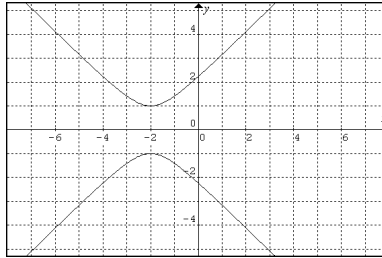
x-int:

$$\left(4 \pm 2\sqrt{2}, 0\right) \approx (6.8, 0), (1.2, 0)$$

y-int:

$$\left(0, 2 \pm 2\sqrt{3}\right) \approx (0, -1.5), (0, 5.5)$$

27.



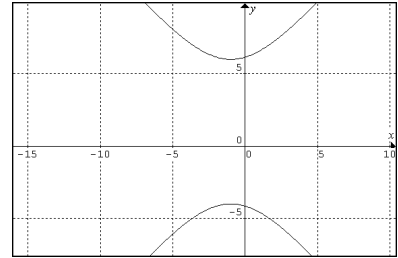
Center: (-2, 0)

Vert: (-2, 1), (-2, -1)

x-int: none

$$y\text{-int: } \left(0, \pm\sqrt{5}\right) \approx (0, \pm 2.2)$$

29.



Center: (-1, 1)

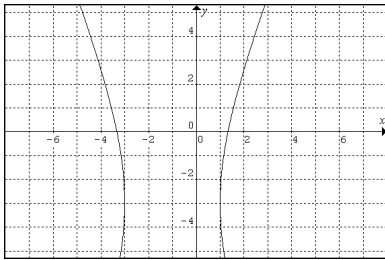
Vert: (-1, -4), (-1, 6)

x-int: none

y-int:

$$\left(0, 1 \pm \frac{5\sqrt{17}}{4}\right) \approx (0, -4.2), (0, 6.2)$$

31.



Center: (-1, -3)

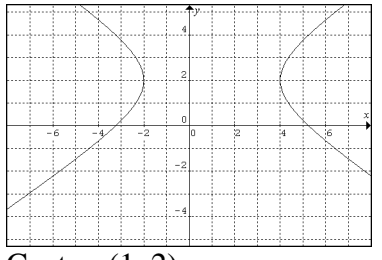
Vert: (1, -3), (-3, -3)

x-int:

$$\left(-1 \pm \frac{2\sqrt{34}}{5}, 0\right) \approx (1.3, 0), (-3.3, 0)$$

y-int: none

33.



Center: (1, 2)

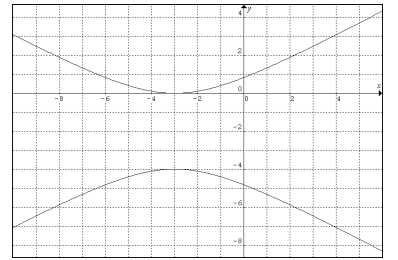
Vert: (-2, 2), (4, 2)

x-int:

$$\left(1 \pm 3\sqrt{2}, 0\right) \approx (5.2, 0), (-3.2, 0)$$

y-int: none

35.



Center: (-3, -2)

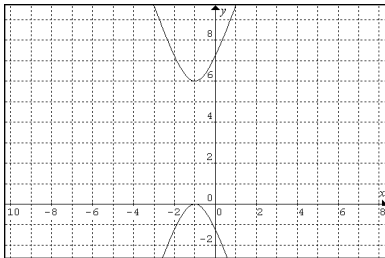
Vert: (-3, 0), (-3, -4)

x-int: (-3, 0)

y-int:

$$\left(0, -2 \pm 2\sqrt{2}\right) \approx (0, -4.8), (0, 0.8)$$

37.



Center: (-1, 3)

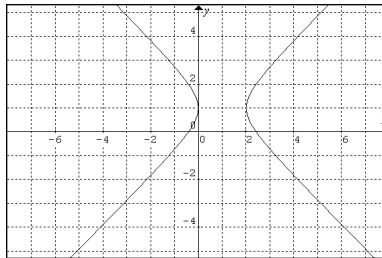
Vert: (-1, 0), (-1, 6)

x-int: (-1, 0)

y-int:

$$\left(0, 3 \pm 3\sqrt{2}\right) \approx (0, -1.2), (0, 7.2)$$

39.



Center: (1, 1)

Vert: (0, 1), (2, 1)

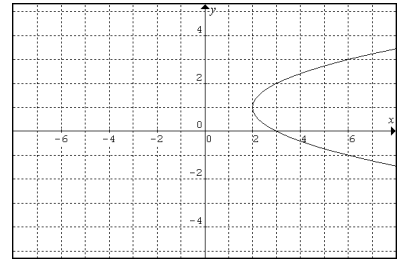
x-int:

$$\left(1 \pm \sqrt{2}, 0\right) \approx (2.4, 0), (-0.4, 0)$$

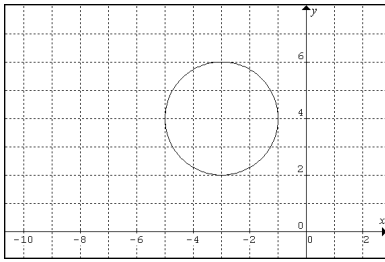
y-int: (0, 1)

41.

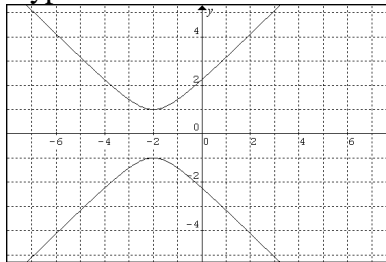
Parabola



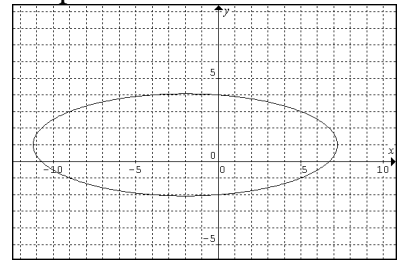
43.
Circle



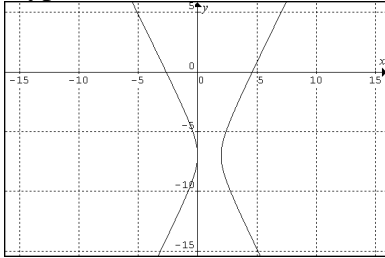
45.
Hyperbola



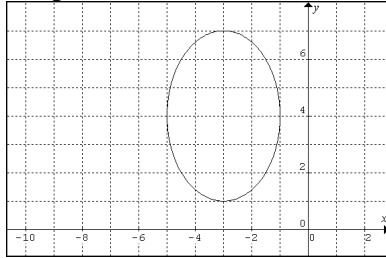
47.
Ellipse



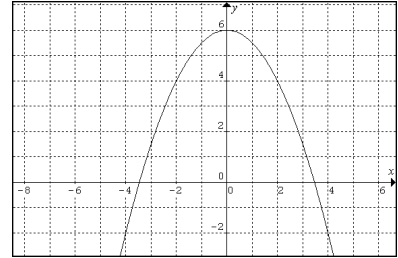
49.
Hyperbola



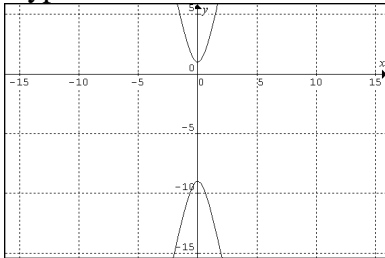
51.
Ellipse



53.
Parabola



55.
Hyperbola



57. $\frac{(x+1)^2}{4} - \frac{(y-2)^2}{9} = 1$

59. $\frac{(y-5)^2}{4} - \frac{21(x+1)^2}{4} = 1$

61. $(y - \frac{7}{2})^2 - (x+1)^2 = 1$ or $(y - \frac{5}{2})^2 - (x+1)^2 = 1$